

Designing Stress-Adaptive Dense Suspensions Using Dynamic Covalent Chemistry

Grayson L. Jackson,* Joseph M. Dennis, Neil D. Dolinski, Michael van der Naald, Hojin Kim, Christopher Eom, Stuart J. Rowan, and Heinrich M. Jaeger



Cite This: *Macromolecules* 2022, 55, 6453–6461



Read Online

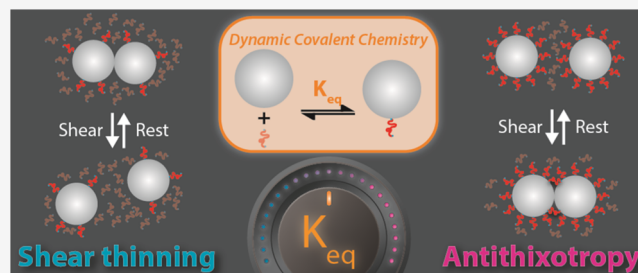
ACCESS |

Metrics & More

Article Recommendations

Supporting Information

ABSTRACT: The non-Newtonian behaviors of dense suspensions are central to their use in technological and industrial applications and arise from a network of particle–particle contacts that dynamically adapt to imposed shear. Reported herein are studies aimed at exploring how dynamic covalent chemistry between particles and the polymeric solvent can be used to tailor such stress-adaptive contact networks, leading to their unusual rheological behaviors. Specifically, a room temperature dynamic thia-Michael bond is employed to rationally tune the equilibrium constant (K_{eq}) of the polymeric solvent to the particle interface. It is demonstrated that low K_{eq} leads to shear thinning, while high K_{eq} produces antithixotropy, a rare phenomenon where the viscosity increases with shearing time. It is proposed that an increase in K_{eq} increases the polymer graft density at the particle surface and that antithixotropy primarily arises from partial debonding of the polymeric graft/solvent from the particle surface and the formation of polymer bridges between particles. Thus, the implementation of dynamic covalent chemistry provides a new molecular handle with which to tailor the macroscopic rheology of suspensions by introducing programmable time dependence. These studies open the door to energy-absorbing materials that not only sense mechanical inputs and adjust their dissipation as a function of time or shear rate but also can switch between these two modalities on demand.



INTRODUCTION

Concentrated or “dense” suspensions of particles in a Newtonian suspending solvent can autonomously sense applied stress and adapt their mechanical properties in response. This feature makes them promising for smart applications in additive manufacturing,^{1–3} coatings and lubrication,^{4,5} vibration dampening,⁶ and impact mitigation.^{7,8} These highly loaded polymer nanocomposites commonly exhibit non-Newtonian flow behaviors, where the viscosity depends on the shear rate or shear stress and may also depend on shearing time. A suspension is termed shear thinning or shear thickening when the viscosity decreases or increases with shear rate, respectively.^{9,10} Additionally, the suspension can be thixotropic if viscosity decreases over time at a fixed shear rate or antithixotropic (also termed negative thixotropic or rheopectic) if it increases over time at a fixed shear rate.¹¹ In particular, antithixotropic materials are attractive because they can transform from liquid-like to solid-like under shear, and the resulting properties of the shear-induced gel such as yield stress¹² and conductivity¹³ can be programmed using their shear history. The ability to controllably tune viscosity (or dissipation) with time would also be relevant to vibration dampening¹⁴ and impact mitigation. However, antithixotropic materials are rare, and few design rules exist to target this unique and useful non-Newtonian behavior.

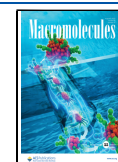
The non-Newtonian rheology of dense suspensions originates from microscopic constraints on interparticle motion.^{5,10,15–21} Shear thinning arises from stress-released constraints, which are broken upon increasing shear rate or stress, whereas stress-activated constraints (formed by increasing shear rate or stress) cause shear thickening. While the macroscopic viscosity in either case is constant at a given shear rate or stress, constraints are constantly breaking and reforming within a structurally dynamic network of noncovalent interparticle contacts. When the viscosity does evolve with time at a constant shear rate as in thixotropy (or antithixotropy), this signals the release (or formation) of constraints.¹¹ While great strides have been made in understanding the constraint-based physics of dense suspensions, an emerging challenge is to connect microscopic constraints to specific chemical interactions.²²

To this end, prior work has focused on manipulating noncovalent chemical interactions such as van der Waals

Received: March 23, 2022

Revised: June 6, 2022

Published: July 20, 2022



forces, solvation forces,^{23–25} depletion attraction,^{26,27} steric stabilization,^{28–31} and hydrogen bonding.^{32–35} These seminal studies provide a conceptual framework to rationalize basic shear-thickening or shear-thinning behavior in terms of the relative strength of particle–particle and particle–solvent interactions (i.e., solubility).^{24,36} If particle–particle attractions cannot be overcome by particle–solvent interactions, then the suspension possesses adhesive constraints at rest, which are broken by shear (shear thinning). If the particle–solvent interaction strength is increased^{24,25,36,37} and the particle–particle attraction is diminished, e.g., using surfactants^{28,29} or a covalently grafted steric barrier,^{30,31} then particles are dispersed at rest yet can form frictionally stabilized contacts under shear (shear thickening). The understanding from this prior work was established using simple noncovalent interactions, yet synthetic organic chemistry offers nearly limitless potential to tune particle–particle and particle–solvent interactions, thus presenting a new frontier for designing responsive dense suspensions.

Dynamic covalent chemistry (DCC) has recently emerged as a method to engineer stress-adaptive functional polymeric materials.^{38–44} Like the noncovalent interactions described above, dynamic covalent bonds are able to dissociate and re-associate under equilibrium conditions, though they typically require a catalyst or external stimulus to access this reversibility.⁴² When integrated into a dynamic covalent network (DCN) or covalent adaptable network (CAN), dynamic bonds enable structural reorganization under mechanical stress. This behavior is quite sensitive to the dynamic equilibrium constant (K_{eq}).^{39,43} Past work also used interfacial DCC to integrate functionalized filler particles into cross-linked resins and studied the stress relaxation of these nanocomposites, though the DCCs used required exogenous catalysts.^{46–50} As opposed to these nanocomposite systems with a cross-linked suspending matrix, dense suspensions possess a fluid matrix that allows particle migration and interparticle constraints to be formed or released under shear. While there have been studies of nanoparticle gels stabilized by dynamic covalent cross-links,^{51–53} these works were primarily concerned with self-assembly rather than shear rheology. Within the context of a dense suspension, an ideal DCC would allow ambient temperature dynamic exchange without a catalyst as well as a readily tunable bond strength (K_{eq}), both of which are achievable using a specific class of thia-Michael (tM) reactions.

The tM reaction is the addition of a thiol to a thia-Michael accepting (tMA) electron-poor olefin to form a thioether adduct.⁵⁴ As demonstrated by foundational small molecule studies,^{55–57} selection of certain substituents adjacent to the double bond can result in catalyst-free dynamic tM bonds at ambient temperatures. Examples of this include benzalcyanoacetate (BCA) and benzalcyanoacetamide (BCAm)-based tMAs. An advantage of BCA or BCAm-based tMAs is that the K_{eq} can be tuned by varying the electron-donating/withdrawing nature of the R-substituents attached to the phenyl ring, which has been exploited in dynamic polymer networks,⁴⁵ adhesives,⁵⁸ and hydrogels.^{59,60}

Taking advantage of the room temperature, catalyst-free, dynamic covalent bonds of the tM reaction with BCAm tMAs, presented here is the first study aimed at exploring the use of DCC in dense suspensions. Specifically, thiol-coated hard-sphere silica particles are dispersed in a fluid matrix composed of a low-molecular-weight BCAm end-capped polymer.

Importantly, this polymeric tMA solvent can form dynamic tM bonds at the particle surface to yield a dynamic brush layer (Figure 1A) with a bonding strength (K_{eq}) orders of

A Dense Dynamic Covalent Suspension (DCS)

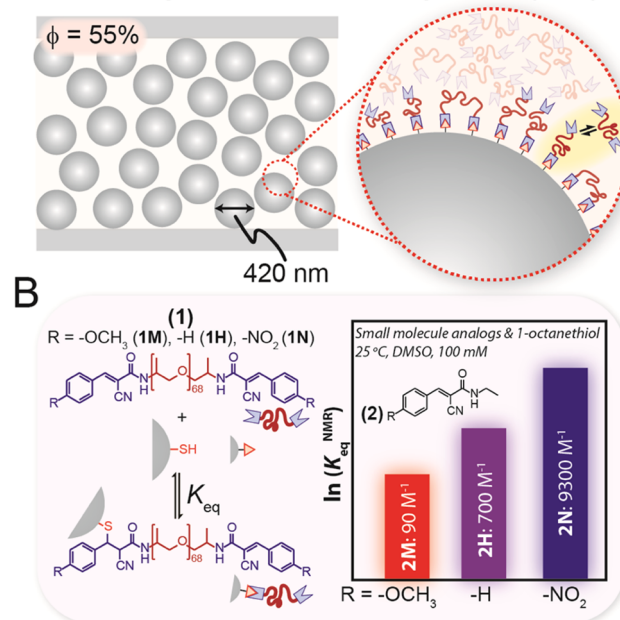


Figure 1. (A) Illustration depicting a dense dynamic covalent suspension (DCS). These high volume fraction ($\phi = 55\%$) DCSs contain particles that can form room temperature dynamic covalent bonds with the surrounding fluid polymer matrix, resulting in a bonded polymer graft layer that exchanges dynamically (inset). (B) Realization of DCSs using dynamic covalent thia-Michael (tM) chemistry. Chemical structure of ditopic poly(propylene glycol) benzalcyanoacetamide (BCAm) thia-Michael acceptors (tMAs) (1) with different R-substituents at the *para*-position of the β -phenyl ring, R = -OCH₃ (1M), -H (1H), -NO₂ (1N). These tMAs can form dynamic tM bonds at the surface of thiol-functionalized particles, which exchange dynamically under ambient conditions without a catalyst. Small molecule analogues (2M, 2H, or 2N) were used to assess how temperature and chemistry affect the dynamic equilibrium constant (K_{eq}^{NMR}).

magnitude larger than is achievable through a single hydrogen bond. While conventional noncovalent dense suspensions (with only hydrogen bonding interactions at the interface) (NCSs) exhibit shear thinning, these dynamic covalent suspensions (DCSs) exhibit antithixotropy, wherein the viscosity reversibly increases under shear and relaxes upon shear cessation. Interestingly, the rheology of DCSs can be tuned between shear thinning and antithixotropy by varying K_{eq} of the tM bond, which in turn affects the dynamic graft density at the particle surface. Moreover, studies of monotopic BCAm tMAs reveal that antithixotropy in DCSs arises from partial debonding of the particle grafts from the surface under shear and the formation of polymer bridges between particles.

RESULTS AND DISCUSSION

Material Synthesis and DCS Preparation. To experimentally realize the concept in Figure 1A, thiol-coated particles were prepared by grafting (3-mercaptopropyl)-trimethoxysilane onto commercially available silica particles using literature procedures (Scheme S1).⁶¹ After surface

functionalization, the particle diameter was 417 ± 30 nm (Figure S1), and the particle surface was covered with 0.5 thiols/nm² as determined by NMR.⁶¹

The tMA end-capped polymer was synthesized in two steps from an amine-terminated $M_n \sim 4000$ g/mol poly(propylene glycol) (PPG) core. Acid-catalyzed condensation with cyanoacetic acid and subsequent Knoevenagel condensation with different benzaldehydes were used to synthesize three ditopic BCAM polymers (Schemes S2 and S3 and Table S1). These are referred to by their R-substituents at the *para*-position of the β -phenyl ring: methoxy ($R = -OCH_3$) (1M), unsubstituted ($R = -H$) (1H), and nitro ($R = -NO_2$) (1N) (Figure 1B).

To understand the baseline effect of temperature and R-substituent on the dynamic equilibrium constant (K_{eq}), small molecule analogues 2M, 2H, and 2N were synthesized, and NMR was used to measure K_{eq}^{NMR} under 100 mM equimolar (with 1-octanethiol) conditions in DMSO- d_6 over the temperature range 25–77 °C (Schemes S4 and S5, Figures S2–S7, and Table S2). These experiments show that the value of K_{eq}^{NMR} can be tuned by over a factor of $\sim 10^3$ using temperature and chemistry: K_{eq}^{NMR} decreases upon heating and, at a constant temperature, shows a trend of $2N > 2H > 2M$ (Figure 1B). As the reaction proceeds through a charged enolate intermediate,⁵⁷ reaction rates and overall equilibrium are expected to be impacted by solvent polarity. In addition to this, K_{eq} for DCSs represents polymeric tMA binding to surface thiols, and the entropic penalty for polymer chain stretching is not accounted for by K_{eq}^{NMR} and would lead to a lower effective K_{eq} in DCSs. With respect to these points, the small molecule controls are treated as estimates; however, the trends in temperature and chemistry from the model studies are expected to translate to DCSs.

DCSs at a silica particle volume fraction (ϕ) of 55% were prepared with either 1M, 1H, or 1N as the suspending solvent to yield DCS-1M, DCS-1H, or DCS-1N. A control non-covalent dense suspension (NCS-OH) was prepared at the same ϕ and with the same particles but with 4000 g/mol hydroxy-terminated PPG as the polymer matrix. From ϕ , particle density, and thiol surface coverage it is estimated that $[-SH] \sim 0.016$ M and $[tMA] \sim 0.46$ M in the liquid phase of these suspensions, a nearly 30-fold excess of the tMA. In other words, the surface thiol group is the limiting reagent and leads to a high bonding fraction and subsequent polymer grafting at the particle surface. The tM adducts are envisioned to serve as a dynamic brush layer that depends on the dynamic bond strength (K_{eq}), with the remaining unbound tMAs serving as the carrier fluid (Figure 1A).

NCS and DCS Rheology. NCS-OH serves as a useful starting point to understand DCS rheology. NCS-OH exhibits conventional shear thinning, where the viscosity decreases with increasing shear rate ($\dot{\gamma}$) (Figure 2A, black trace). In this figure, the reduced viscosity η_r ($\eta_r = \eta_{apparent}/\eta_0$, where η_0 is the Newtonian viscosity of the suspending solvent and $\eta_{apparent}$ is the suspension viscosity measured by the rheometer) is used to isolate the viscosity contribution of the particles from that of the suspending polymeric solvent (Figure S8). See the Supporting Information for a discussion of measurement artifacts and Figure S9, which shows all rheology was conducted within measurable limits.⁶² The forward (increasing) and backward (decreasing) shear rate ramps overlay quite well for NCS-OH, illustrating no processing hysteresis and viscosity which is independent of shearing time. As explored by

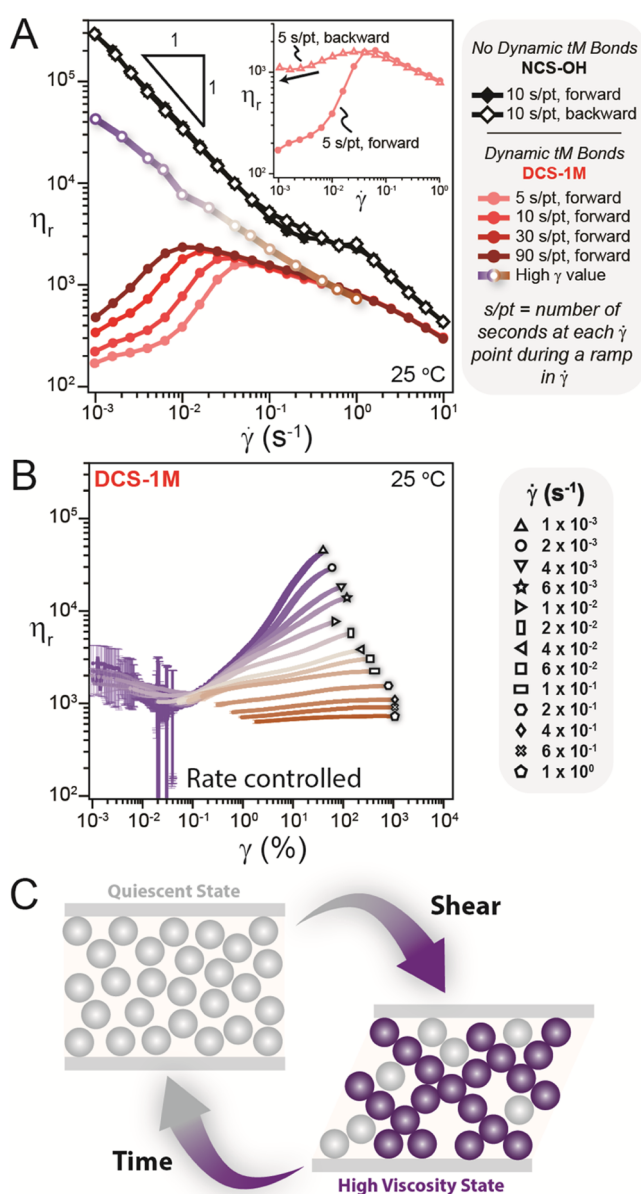


Figure 2. (A) Suspensions with only noncovalent hydrogen bonding interactions between particles and solvent (NCS-OH) exhibit reversible shear thinning. In contrast, dynamic covalent suspensions such as DCS-1M exhibit antithixotropy. Reduced viscosity η_r versus shear rate ($\dot{\gamma}$) for DCS-1M with different waiting times (s/pt is the number of seconds at each $\dot{\gamma}$ point during a ramp in $\dot{\gamma}$) reveal that η_r increases as a function of shearing time and eventually approaches a steady state. Similarly, a comparison of the increasing (forward) and decreasing (backward) $\dot{\gamma}$ ramps reveals hysteresis (inset). The error bars are approximately the size of the plot markers and represent the standard deviation of three forward or backward shear rate sweeps. (B) Evolution of η_r as a function of strain (γ) at a constant $\dot{\gamma}$. The error bars here represent the standard deviation of the viscosity (see the Supporting Information for details). (C) Schematic depiction of antithixotropy, wherein shear reversibly transforms a low viscosity quiescent state into a higher viscosity state through the formation of a stress-bearing particle network (purple).

others,^{19,24,36} shear-thinning behavior in systems like NCS-OH can be understood as a solubility mismatch wherein hydrogen bonding or van der Waals forces between particle and solvent are not strong enough to overcome interparticle attractions.

This leads to a stress-bearing (i.e., high viscosity) network of adhesive particle–particle contacts at rest, which is disrupted by shear and leads to shear thinning.^{15,29} These stress-released interparticle contacts rapidly re-form upon shear cessation, and the suspension viscosity does not strongly depend on the shear history.

In stark contrast to the conventional shear thinning of NCS-OH, introduction of dynamic tM chemistry at the particle surface in DCS-1M leads to rich time-dependent rheology (Figure 2A). The measured viscosity on the forward shear rate ramp is low, while it is much higher upon the backward shear rate ramp, indicating a strong hysteresis (Figure 2A, inset). However, the higher viscosity state decays upon shear cessation. Increasing the waiting time at each point in the shear rate ramp leads to a higher measured viscosity at low shear rates, while the data were identical at higher shear rates (Figure 2A). At a constant shear rate, the viscosity evolves as a function of strain (γ) and shows an initial decay from the presheared state followed by growth and appears to be plateauing to a high γ value (Figure 2B). The viscosity at the largest measured strain, which for $\dot{\gamma} < 0.1 \text{ s}^{-1}$, is an underestimate of the true “steady-state” viscosity, is plotted in Figure 2A and decreases with increasing shear rate. This trend is also apparent when comparing the viscosity for different shear rates at a constant γ value (Figure S10). DCS-1M exhibits stronger shear-thinning behavior as γ increases, suggesting a steady-state shear-thinning behavior. This conclusion is also supported by constant stress (creep) measurements of DCS-1M revealing a viscosity bifurcation:^{12,63} the viscosity diverges for $\sigma \leq 10 \text{ Pa}$ and flows for $\sigma \geq 100 \text{ Pa}$ (Figure S11). Under shear rate control, this manifests as a viscosity that grows at a constant shear rate and then plateaus to the viscosity at which the applied shear stress is equivalent to the yield stress of the network. In other words, DCS-1M exhibits a yield stress but only under shear. Qualitatively similar behavior was observed in constant shear rate and creep measurements of DCS-1H (Figure S12) and DCS-1N (Figure S13). This reversible increase in viscosity indicates that these DCSs are antithixotropic, i.e., the opposite of more conventional thixotropy, where shear forms a stress-bearing particle network that returns to its equilibrium quiescent state upon shear cessation (Figure 2C).^{4,11}

Small-amplitude oscillatory shear (SAOS) was used to track the decay of the complex viscosity (η^*) to understand how these shear-induced structures in DCSs relax upon shear cessation (Figure S14). These SAOS experiments were conducted immediately following the constant shear rate experiments shown in Figures 2B, S12, and S13 (see Figure S14 for experimental protocol). DCSs subjected to lower shear rates, which typically had larger η_r plateau values prior to SAOS, exhibited a slower decay of η^* . In other words, more robust particle contact networks prior to shear cessation typically persisted longer once oscillatory shear was applied. It is worth pointing out that for shear-induced networks with similar η_r , the decay of η^* does not clearly correlate with dynamic bond K_{eq} but does coincide with the trend in the viscosity of the dynamic tMA oil matrix (generally the slowest for DCS-1N, followed by DCS-1M, and then DCS-1H). This observation suggests that polymer diffusion also plays a role in the relaxation process.

Tuning Macroscopic Rheology with K_{eq} . As indicated by the small molecule studies (Figures 1B and S7), K_{eq} and the dynamic brush layer density in DCSs can be systematically

varied using temperature and chemistry. As such, temperature-dependent rheology of DCSs was performed over the range 0–80 °C, and shear rate ramps were used to identify antithixotropy or lack thereof (Figures 3A, S15, and S16). These hard-sphere silica particles are considered nonswellable, and thus the particle core volume fraction remains constant over this temperature window. As expected, NCS-OH exhibits reversible shear thinning or mild thixotropy over the entire temperature range (Figure S15). However, the DCSs are much more sensitive to temperature and changes in K_{eq} . While DCS-1M exhibits antithixotropy at 10 °C (Figure S16) and 30 °C, decreasing K_{eq} by heating ≥ 40 °C leads to strong and reversible shear thinning with a slope of nearly -1 on a log–log plot of η_r vs $\dot{\gamma}$ (Figure 3A). At 70 °C, it is apparent that η_r at a given shear rate is significantly larger even than that reached in the high $\dot{\gamma}$ limit at 25 °C. In other words, the stress-bearing particle network formed at rest at 70 °C is stronger than that formed under shear at 25 °C. A similar transition from antithixotropy to shear thinning with mild thixotropy is observed when heating DCS-1H, but the transition occurs when heating between 60 and 70 °C (Figure 3A). The area of the hysteresis loop generally decreases upon heating DCS-1M or DCS-1H, which could reflect a gradual transition between antithixotropy and shear thinning. The larger K_{eq} for DCS-1N leads to antithixotropy over the entire investigated range with an increasing mismatch between the forward and backward shear rate ramps. This trend for DCS-1N is particularly obvious at 70 °C, where the viscosity at the end of the hysteresis loop is 3 orders of magnitude larger than its initial value.

Grouping the data shown in Figure 3A in terms of K_{eq}^{NMR} determined from small molecule analogues (Figure S7) yields the rheological state diagram shown in Figure 3B. Despite the potential issues in translating K_{eq}^{NMR} directly to DCSs discussed above, the data in Figure 3B show a clear transition between antithixotropy and shear thinning at roughly the same value of K_{eq}^{NMR} ($\sim 50 \text{ M}^{-1}$) whether chemistry or temperature is used as the input variable. DCS-1N never reaches a low enough K_{eq}^{NMR} value to cross the threshold and thus only shows antithixotropy, whereas heating DCS-1M or DCS-1H leads to shear thinning. Antithixotropy in DCSs is accompanied by viscoelastic or liquid-like behavior under SAOS, while shear-thinning DCSs are solid-like (Figures S17 and S18). It is worth pointing out that the estimated K_{eq}^{NMR} value for NCS-OH (Table S2) is orders of magnitude below the $\sim 50 \text{ M}^{-1}$ threshold, and this system only exhibits reversible shear thinning.

The effect of K_{eq} in DCSs and transition from antithixotropy can be understood in terms of changes to the surface grafting density (Figure 3C), which alters particle stability in the surrounding homopolymer matrix in the quiescent, unsheared state. As detailed in the Supporting Information, K_{eq}^{NMR} can be converted into a fraction of bonded thiols (p). Again, this p -value likely overestimates the bonding of polymeric tMAs to a surface due to the entropic penalty for polymer chain stretching but serves as a useful proxy for the dynamic graft density in DCSs (Figure 3C). Interestingly, p shows a precipitous drop in the vicinity of $K_{eq}^{NMR} \sim 50 \text{ M}^{-1}$, where DCSs transition from antithixotropy to shear thinning.

Such a change in nanoparticle dispersibility with grafting density is preceded for covalently grafted polymer brushes. Polymer-grafted nanoparticle (PGNP) stability in a polymer melt depends on grafting density and the relative length of the

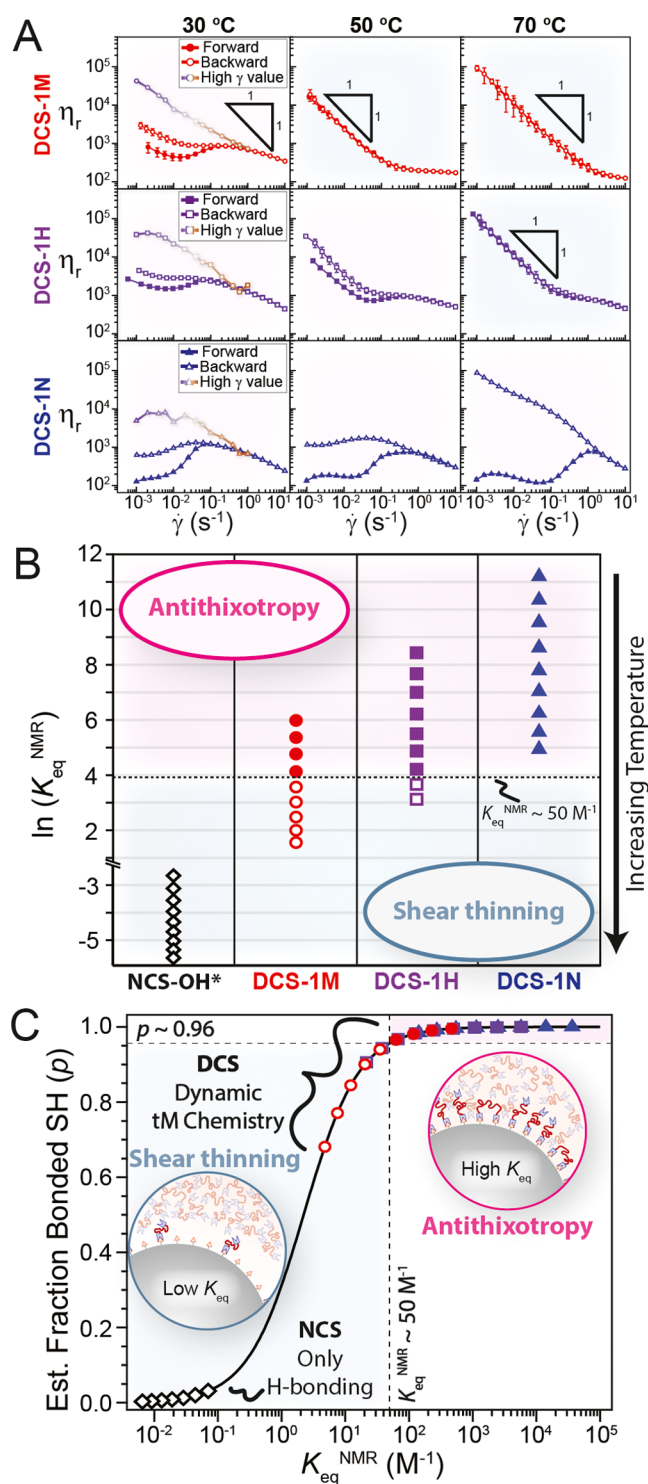


Figure 3. (A) η_r versus $\dot{\gamma}$ for forward (filled symbols) and backward (open symbols) ramps waiting 10 s at each $\dot{\gamma}$ point during a ramp in $\dot{\gamma}$ reveal either hysteresis (antithixotropy) or no hysteresis (shear thinning). Error bars for forward–backward shear rate ramps represent the standard deviation of three forward or backward shear rate sweeps. Error bars for the high γ values are approximately the size of the plot markers. (B) Rheological state diagram for 0–80 °C for each system showing a transition from antithixotropy (filled symbols) to shear thinning (open symbols) at $K_{eq}^{NMR} \sim 50$ M $^{-1}$. K_{eq}^{NMR} for NCS-OH was estimated using literature data (see Table S2). (C) Relating K_{eq}^{NMR} to an estimated mole fraction of bound thiol (p), which serves as a proxy for the brush layer density (solid line, see the Supporting

Figure 3. continued

Information for more details). Symbol identities are the same as in (B).

grafted and matrix polymer chains.^{64–66} In the special case where the graft and matrix polymer chains are the same length (as is the case here), too low of a grafting density leads to partial wetting of the brush by the matrix, and too high of a grafting density causes brush dewetting or a “dry” brush. Both cases lead to particle aggregation due to an entropic depletion attraction. In contrast, intermediate grafting density leads to a wet brush and provides a repulsive barrier and particle dispersal.

Extending these lessons from covalent brushes to dynamic covalent brushes, K_{eq} controls the time-averaged graft density (p) (Figure 3C). A large p leads to an initially dispersed quiescent state, as evidenced by the relatively low initial η_r (Figure 3A) and liquid-like or viscoelastic SAOS response (Figures S17 and S18). Decreasing K_{eq} below ~ 50 M $^{-1}$ leads to a precipitous drop in p , which drives particle–particle contacts at rest,^{24,29,36} as evidenced by the higher η_r , shear thinning under steady shear, and solid-like SAOS response (Figures 3A, S17, and S18).^{19,65} As unbonded surface thiol groups could potentially ionize, we note that the drop in p and transition from antithixotropy to shear thinning could also be related to an increase in particle surface charge, which alters nanoparticle dynamics⁶⁷ and stability within the homopolymer melt. The system would be expected to be in the concentrated polymer brush (CPB) regime from a minimum graft density of ~ 0.07 chains/nm 2 to the maximum theoretical graft density of 0.5 chains/nm 2 set by the interfacial –SH density.^{68,69}

The analogy to PGNPs applies to the initial quiescent state of the suspension (i.e., dispersed or aggregated) but does not answer why antithixotropy is observed for DCSs under steady shear. Antithixotropy requires shear-induced contacts, which could either be stabilized by polymer bridging or interparticle frictional contacts. Shear-induced polymer bridging would be possible in DCSs with ditopic tMAs and has been reported in “shake gels” of small ~ 20 nm particles with high molecular weight $\sim 10^6$ g/mol polymers.^{70–74} On the other hand, antithixotropy is also possible without bridging interactions due to particle–particle frictional contacts, as seen in suspensions with high aspect ratio particles.^{12,75,76} Frictional contacts would be possible in DCSs if the dynamic brush were to debond from the particle surface under shear and allow interparticle contacts.

To understand whether the primary mechanism for antithixotropy in DCSs involves polymer bridging or frictional particle–particle contacts, monotopic tMAs 3M and 3N (incapable of bridging) were synthesized (Figure 4A). As the molecular weight of the monotopic 3 is nominally half that of the ditopic 1, both systems possess roughly the same stoichiometric imbalance of tMA to thiol at a constant solids volume fraction of $\phi = 55\%$. As shown in Figure 4B, DCS-3N exhibits shear thinning at low shear rates, followed by shear thickening past ~ 1 s $^{-1}$. Essentially, no hysteresis is observed for DCS-3N, and the backward flow curve almost exactly matches the high γ viscosity value (Figure S19). In contrast, the same experimental conditions for DCS-1N lead to pronounced hysteresis over a larger shear rate range. The slight hysteresis at low shear rates observed for DCS-3N is also

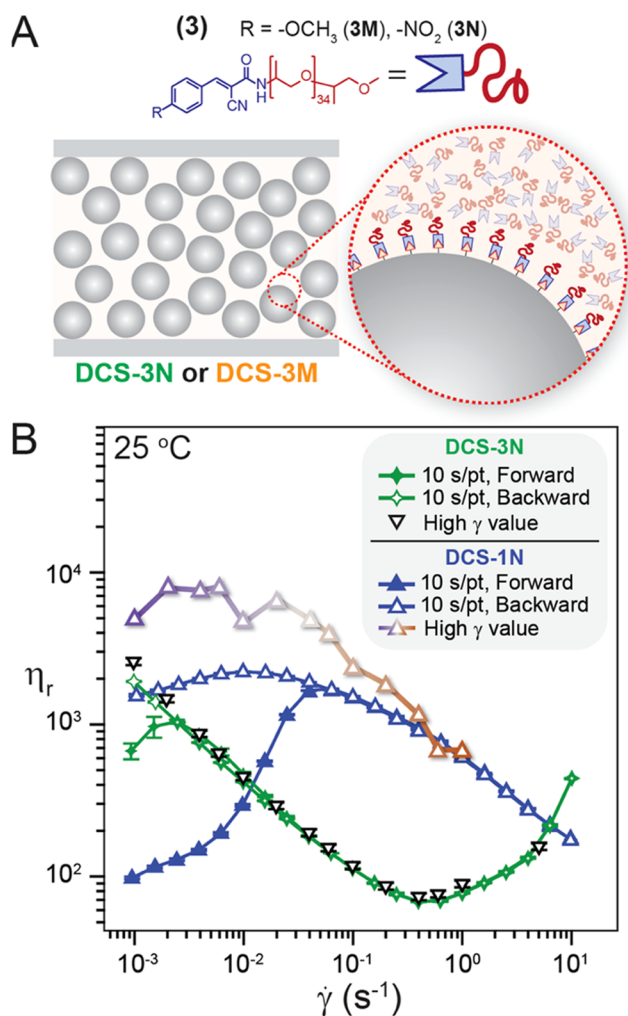


Figure 4. (A) Monotopic tMA 3N or 3M leads to DCSs without the possibility of shear-induced bridging between particles. (B) Reduced viscosity (η_r) for a forward–backward shear rate ($\dot{\gamma}$) ramp (10 s/pt measurement time) reveals mostly reversible behavior for DCS-3N, with a backward shear rate ramp that nearly matches the high γ viscosity (Figure S19). This behavior contrasts greatly with that of the DCS-1N, which shows pronounced hysteresis. The high γ reduced viscosity for DCS-3N is also much lower than that of DCS-1N at a given shear rate. See Figure S19 for a comparison of DCS-3M with DCS-1M. The error bars (on the order of the marker size) were determined as described in Figures 2 and 3.

observed for a NCS prepared with $M_n \sim 2000$ g/mol hydroxy-terminated PPG (Figure S19), indicating that the dynamic covalent chemistry of monotopic tMAs does not induce hysteresis. Along the same lines, DCS-3N and DCS-3M equilibrate to their high γ viscosities at orders of magnitude lower strain values (Figure S19) than DCS-1N (Figure S13) or DCS-1M (Figure 2), respectively. Therefore, the pronounced hysteresis for ditopic tMAs is primarily the result of shear-induced polymer bridging.

Additionally, the ditopic DCSs exhibit much larger high γ viscosities than their monotopic counterparts. Even after accounting for the differences in the tMA oil viscosity, the high γ η_r for the monotopic DCSs at a given shear rate is ~ 20 times lower than for the ditopic DCSs (Figures 4B and S19). The larger high γ viscosities for ditopic DCSs could indicate an additional attractive force between particles,¹⁹ which would be expected with shear-induced polymer bridging.

While further experiments are needed to fully understand the effects of dynamic graft molecular weight and stoichiometric imbalance, the comparison between monotopic and ditopic tMAs demonstrates that antithixotropy in ditopic DCSs primarily results from shear-induced polymer bridging (Figure 5). Such a mechanism requires not only polymer grafts

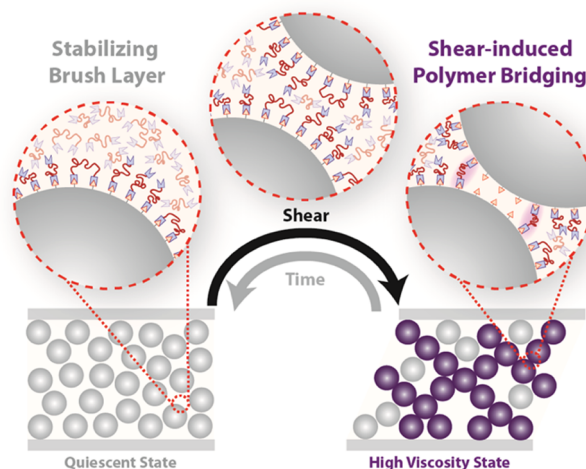


Figure 5. Cartoon illustration of the primary microscopic mechanism for antithixotropy in DCSs. Initially dispersed particles are forced into close contact by applied shear, during which the dynamic brush layer can partially debond and enable shear-induced polymer bridges, which stabilize the high viscosity state. Removal of shear regenerates the sterically stabilized low viscosity quiescent state via re-bonding of free tMAs to re-form a repulsive brush layer.

capable of dynamically bridging between particle surfaces but also exposed (“bare”) surface sites which are dynamically revealed by tM debonding. In this scenario, the increasing hysteresis for DCS-1N at elevated temperatures could be explained by a slight reduction in the dynamic graft density (p), which allows a larger number of polymer bridges. Prior work on dense suspensions¹⁰ has shown that contact friction,⁷⁷ surface roughness,⁷⁸ hydrodynamics,⁷⁹ and attraction²⁶ contribute to non-Newtonian flow behaviors and could play a role in this system. For instance, Craig and co-workers have demonstrated that tensile force accelerates the dissociation rate in dynamic metal–ligand complexes,^{80,81} meaning that hydrodynamic shear stress at the particle surface could play a role in accelerating tM debonding and exposing surface sites under shear. In other words, p may decrease as the shear rate increases. Such tensile forces could also be responsible for the shear-thinning behavior of the antithixotropic networks at high shear rates as a large enough shear stress releases particles from their microscopic tethers before they can re-form. Finally, the decay of the antithixotropic state upon shear cessation (Figure S14) correlates with the viscosity of the particle network before decay, with a lesser dependence on the viscosity of the dynamic tMA oil matrix. These data suggest that once the polymer bridges have stabilized the shear-induced network, contact relaxation requires particles to separate and subsequent re-infiltration of free tMA polymers to regenerate the repulsive brush layer (Figure 5).

CONCLUSIONS

The use of dynamic covalent thia-Michael chemistry at the particle–solvent interface has been shown to be a new

approach to control the macroscopic flow behavior of dense suspensions. Small molecule control experiments were used to understand how temperature and chemistry control the equilibrium bonding constant (K_{eq}). DCSs with a high K_{eq} exhibit antithixotropy, a rare non-Newtonian behavior, where viscosity increases with shearing time and relaxes upon shear cessation. Decreasing K_{eq} in these DCSs led to more conventional rheology such as shear thinning. The changes in rheology with K_{eq} are interpreted in terms of the polymer graft density at the particle surface and subsequent wetting behavior by the surrounding homopolymer matrix. Finally, monotopic tMAs were used to elucidate the primary mechanism of DCS antithixotropy, namely, that the dynamic covalent brush layer partially debonds under shear to enable polymer bridges between particles.

Incorporation of dynamic covalent grafts at a particle surface provides a new path forward toward the general design of antithixotropic materials, which can controllably adjust their dissipation over time in response to mechanical inputs. Furthermore, the tunability of this particular system enables temperature to control the polymer graft density *in situ* and further toggle between two types of non-Newtonian behaviors, antithixotropy and shear thinning. This fine level of control over energy absorption and dissipation opens the door to new materials for vibration dampening, shock absorption, and impact mitigation.

■ ASSOCIATED CONTENT

SI Supporting Information

The Supporting Information is available free of charge at <https://pubs.acs.org/doi/10.1021/acs.macromol.2c00603>.

Experimental details, synthetic schemes, suspension preparation, small molecule control experiments, creep and constant shear rate measurements, decay of the antithixotropic state, temperature-dependent rheology for NCS-OH, and SAOS data and SAOS state diagram for all ditopic systems (PDF)

■ AUTHOR INFORMATION

Corresponding Author

Grayson L. Jackson – James Franck Institute, University of Chicago, Chicago, Illinois 60637, United States;
orcid.org/0000-0003-0663-3274;
Email: graysonjacksonphd@gmail.com

Authors

Joseph M. Dennis – Combat Capabilities and Development Command, Army Research Laboratory, Aberdeen Proving Ground, Maryland 21005, United States

Neil D. Dolinski – Pritzker School of Molecular Engineering, University of Chicago, Chicago, Illinois 60637, United States; orcid.org/0000-0002-2160-8811

Michael van der Naald – James Franck Institute, University of Chicago, Chicago, Illinois 60637, United States; Department of Physics, University of Chicago, Chicago, Illinois 60637, United States

Hojin Kim – James Franck Institute, University of Chicago, Chicago, Illinois 60637, United States; Pritzker School of Molecular Engineering, University of Chicago, Chicago, Illinois 60637, United States; orcid.org/0000-0001-5922-2490

Christopher Eom – Pritzker School of Molecular Engineering, University of Chicago, Chicago, Illinois 60637, United States
Stuart J. Rowan – Pritzker School of Molecular Engineering, University of Chicago, Chicago, Illinois 60637, United States; Department of Chemistry, University of Chicago, Chicago, Illinois 60637, United States; Chemical and Engineering Sciences Division, Argonne National Laboratory, Lemont, Illinois 60439, United States; orcid.org/0000-0001-8176-0594

Heinrich M. Jaeger – James Franck Institute, University of Chicago, Chicago, Illinois 60637, United States; Department of Physics, University of Chicago, Chicago, Illinois 60637, United States

Complete contact information is available at:

<https://pubs.acs.org/10.1021/acs.macromol.2c00603>

Author Contributions

The manuscript was written through contributions of all authors. All authors have given approval to the final version of the manuscript.

Notes

The authors declare no competing financial interest.

Safety statement: no unexpected or unusual safety hazards were encountered in the work reported.

■ ACKNOWLEDGMENTS

The authors acknowledge support from the Center for Hierarchical Materials Design (CHiMaD) under Award Number 70NANB19H005 (US Department of Commerce). Additional support was provided by the Army Research Laboratory and was accomplished under Cooperative Agreement Number W911NF-20-2-0044. The views and conclusions contained in this document are those of the authors and should not be interpreted as representing the official policies, either expressed or implied, of the Army Research Laboratory or the U.S. Government. The U.S. Government is authorized to reproduce and distribute reprints for Government purposes, notwithstanding any copyright notation herein. Support from the Army Research Office under DURIP Grant W911NF-21-1-0038 and the Division of Materials Research of the NSF (Award #2104694) are also gratefully acknowledged. This work made use of the shared facilities at the University of Chicago Materials Research Science and Engineering Center (MRSEC), supported by the National Science Foundation under Award Number DMR-2011854. N.D.D. thanks the Pritzker School of Molecular Engineering for support through a postdoctoral fellowship. The authors thank Abhinendra Singh and Josh Mysona for stimulating discussions and the Huntsman Corporation for their donation of Jeffamine M-2005 as the starting material for compound 3.

■ REFERENCES

- (1) M'Barki, A.; Bocquet, L.; Stevenson, A. Linking Rheology and Printability for Dense and Strong Ceramics by Direct Ink Writing. *Sci. Rep.* **2017**, 7, No. 6017.
- (2) Sun, K.; Wei, T.-S.; Ahn, B. Y.; Seo, J. Y.; Dillon, S. J.; Lewis, J. A. 3D Printing of Interdigitated Li-Ion Microbattery Architectures. *Adv. Mater.* **2013**, 25, 4539–4543.
- (3) Nelson, A. Z.; Schweizer, K. S.; Rauzan, B. M.; Nuzzo, R. G.; Vermant, J.; Ewoldt, R. H. Designing and Transforming Yield-Stress Fluids. *Curr. Opin. Solid State Mater. Sci.* **2019**, 23, No. 100758.
- (4) Barnes, H. A. Thixotropy—a Review. *J. Non-Newtonian Fluid Mech.* **1997**, 70, 1–33.

- (5) Bonn, D.; Denn, M. M.; Berthier, L.; Divoux, T.; Manneville, S. Yield Stress Materials in Soft Condensed Matter. *Rev. Mod. Phys.* **2017**, *89*, No. 035005.
- (6) Stanway, R.; Sproston, J. L.; El-Wahed, A. K. Applications of Electro-Rheological Fluids in Vibration Control: A Survey. *Smart Mater. Struct.* **1996**, *5*, 464–482.
- (7) Petel, O. E.; Ouellet, S.; Loiseau, J.; Marr, B. J.; Frost, D. L.; Higgins, A. J. The Effect of Particle Strength on the Ballistic Resistance of Shear Thickening Fluids. *Appl. Phys. Lett.* **2013**, *102*, No. 064103.
- (8) Lee, Y. S.; Wetzel, E. D.; Wagner, N. J. The Ballistic Impact Characteristics of Kevlar Woven Fabrics Impregnated with a Colloidal Shear Thickening Fluid. *J. Mater. Sci.* **2003**, *38*, 2825–2833.
- (9) Brown, E.; Jaeger, H. M. Shear Thickening in Concentrated Suspensions: Phenomenology, Mechanisms and Relations to Jamming. *Rep. Prog. Phys.* **2014**, *77*, No. 046602.
- (10) Ness, C.; Seto, R.; Mari, R. The Physics of Dense Suspensions. *Annu. Rev. Condens. Matter Phys.* **2022**, *13*, 97–117.
- (11) Mewis, J.; Wagner, N. J. Thixotropy. *Adv. Colloid Interface Sci.* **2009**, *147–148*, 214–227.
- (12) Ovarlez, G.; Tocquer, L.; Bertrand, F.; Coussot, P. Rheopexy and Tunable Yield Stress of Carbon Black Suspensions. *Soft Matter* **2013**, *9*, 5540–5549.
- (13) Narayanan, A.; Mugele, F.; Duits, M. H. G. Mechanical History Dependence in Carbon Black Suspensions for Flow Batteries: A Rheo-Impedance Study. *Langmuir* **2017**, *33*, 1629–1638.
- (14) Oates, K. M. N.; Krause, W. E.; Jones, R. L.; Colby, R. H. Rheopexy of Synovial Fluid and Protein Aggregation. *J. R. Soc. Interface* **2006**, *3*, 167–174.
- (15) Guy, B. M.; Richards, J. A.; Hodgson, D. J. M.; Blanco, E.; Poon, W. C. K. Constraint-Based Approach to Granular Dispersion Rheology. *Phys. Rev. Lett.* **2018**, *121*, No. 128001.
- (16) Lin, N. Y. C.; Guy, B. M.; Hermes, M.; Ness, C.; Sun, J.; Poon, W. C. K.; Cohen, I. Hydrodynamic and Contact Contributions to Continuous Shear Thickening in Colloidal Suspensions. *Phys. Rev. Lett.* **2015**, *115*, No. 228304.
- (17) Denn, M. M.; Morris, J. F.; Bonn, D. Shear Thickening in Concentrated Suspensions of Smooth Spheres in Newtonian Suspending Fluids. *Soft Matter* **2018**, *14*, 170–184.
- (18) Singh, A.; Pednekar, S.; Chun, J.; Denn, M. M.; Morris, J. F. From Yielding to Shear Jamming in a Cohesive Frictional Suspension. *Phys. Rev. Lett.* **2019**, *122*, No. 098004.
- (19) Nabizadeh, M.; Jamali, S. Life and Death of Colloidal Bonds Control the Rate-Dependent Rheology of Gels. *Nat. Commun.* **2021**, *12*, No. 4274.
- (20) Fernandez, N.; Mani, R.; Rinaldi, D.; Kadau, D.; Mosquet, M.; Lombois-Burger, H.; Cayer-Barrioz, J.; Herrmann, H. J.; Spencer, N. D.; Isa, L. Microscopic Mechanism for Shear Thickening of Non-Brownian Suspensions. *Phys. Rev. Lett.* **2013**, *111*, No. 108301.
- (21) Royer, J. R.; Blair, D. L.; Hudson, S. D. Rheological Signature of Frictional Interactions in Shear Thickening Suspensions. *Phys. Rev. Lett.* **2016**, *116*, No. 188301.
- (22) Singh, A.; Jackson, G. L.; van der Naald, M.; de Pablo, J. J.; Jaeger, H. M. Stress-Activated Constraints in Dense Suspension Rheology. *Phys. Rev. Fluids* **2022**, *7*, No. 054302.
- (23) van der Naald, M.; Zhao, L.; Jackson, G. L.; Jaeger, H. M. The Role of Solvent Molecular Weight in Shear Thickening and Shear Jamming. *Soft Matter* **2021**, *17*, 3144–3152.
- (24) Raghavan, S. R.; Walls, H. J.; Khan, S. A. Rheology of Silica Dispersions in Organic Liquids: New Evidence for Solvation Forces Dictated by Hydrogen Bonding. *Langmuir* **2000**, *16*, 7920–7930.
- (25) Ueno, K.; Imaizumi, S.; Hata, K.; Watanabe, M. Colloidal Interaction in Ionic Liquids: Effects of Ionic Structures and Surface Chemistry on Rheology of Silica Colloidal Dispersions. *Langmuir* **2009**, *25*, 825–831.
- (26) Gopalakrishnan, V.; Zukoski, C. F. Effect of Attractions on Shear Thickening in Dense Suspensions. *J. Rheol.* **2004**, *48*, 1321–1344.
- (27) Park, N.; Rathee, V.; Blair, D. L.; Conrad, J. C. Contact Networks Enhance Shear Thickening in Attractive Colloid-Polymer Mixtures. *Phys. Rev. Lett.* **2019**, *122*, No. 228003.
- (28) Brown, E.; Forman, N. A.; Orellana, C. S.; Zhang, H.; Maynor, B. W.; Betts, D. E.; DeSimone, J. M.; Jaeger, H. M. Generality of Shear Thickening in Dense Suspensions. *Nat. Mater.* **2010**, *9*, 220–224.
- (29) Richards, J. A.; O'Neill, R. E.; Poon, W. C. K. Turning a Yield-Stress Calcite Suspension into a Shear-Thickening One by Tuning Inter-Particle Friction. *Rheol. Acta* **2021**, *60*, 97–106.
- (30) Guy, B. M.; Hermes, M.; Poon, W. C. K. Towards a Unified Description of the Rheology of Hard-Particle Suspensions. *Phys. Rev. Lett.* **2015**, *115*, No. 088304.
- (31) Frith, W. J.; d'Haene, P.; Buscall, R.; Mewis, J. Shear Thickening in Model Suspensions of Sterically Stabilized Particles. *J. Rheol.* **1996**, *40*, 531–548.
- (32) James, N. M.; Han, E.; de la Cruz, R. A. L.; Jureller, J.; Jaeger, H. M. Interparticle Hydrogen Bonding Can Elicit Shear Jamming in Dense Suspensions. *Nat. Mater.* **2018**, *17*, 965–970.
- (33) Yang, W.; Wu, Y.; Pei, X.; Zhou, F.; Xue, Q. Contribution of Surface Chemistry to the Shear Thickening of Silica Nanoparticle Suspensions. *Langmuir* **2017**, *33*, 1037–1042.
- (34) Warren, J.; Offenberger, S.; Toghiani, H.; Pittman, C. U.; Lacy, T. E.; Kundu, S. Effect of Temperature on the Shear-Thickening Behavior of Fumed Silica Suspensions. *ACS Appl. Mater. Interfaces* **2015**, *7*, 18650–18661.
- (35) Laun, H. M. Rheological Properties of Aqueous Polymer Dispersions. *Angew. Makromol. Chem.* **1984**, *123*, 335–359.
- (36) Raghavan, S. R.; Hou, J.; Baker, G. L.; Khan, S. A. Colloidal Interactions between Particles with Tethered Nonpolar Chains Dispersed in Polar Media: Direct Correlation between Dynamic Rheology and Interaction Parameters. *Langmuir* **2000**, *16*, 1066–1077.
- (37) Bourrianne, P.; Vincent, N.; Polly, G.; Divoux, T.; McKinley, G. H. Tuning the Shear-Thickening of Suspensions through Surface Roughness and Physico-Chemical Interactions, 2020. arXiv:2001.02290. <https://arxiv.org/abs/2001.02290>.
- (38) Wojtecki, R. J.; Meador, M. A.; Rowan, S. J. Using the Dynamic Bond to Access Macroscopically Responsive Structurally Dynamic Polymers. *Nat. Mater.* **2011**, *10*, 14–27.
- (39) Kloxin, C. J.; Bowman, C. N. Covalent Adaptable Networks: Smart, Reconfigurable and Responsive Network Systems. *Chem. Soc. Rev.* **2013**, *42*, 7161–7173.
- (40) Chakma, P.; Rodrigues Possarle, L. H.; Digby, Z. A.; Zhang, B.; Sparks, J. L.; Konkolewicz, D. Dual Stimuli Responsive Self-Healing and Malleable Materials Based on Dynamic Thiol-Michael Chemistry. *Polym. Chem.* **2017**, *8*, 6534–6543.
- (41) Jing, B. B.; Evans, C. M. Catalyst-Free Dynamic Networks for Recyclable, Self-Healing Solid Polymer Electrolytes. *J. Am. Chem. Soc.* **2019**, *141*, 18932–18937.
- (42) Rowan, S. J.; Cantrill, S. J.; Cousins, G. R. L.; Sanders, J. K. M.; Stoddart, J. F. Dynamic Covalent Chemistry. *Angew. Chem., Int. Ed.* **2002**, *41*, 898–952.
- (43) Yount, W. C.; Loveless, D. M.; Craig, S. L. Small-Molecule Dynamics and Mechanisms Underlying the Macroscopic Mechanical Properties of Coordinatively Cross-Linked Polymer Networks. *J. Am. Chem. Soc.* **2005**, *127*, 14488–14496.
- (44) Xu, D.; Craig, S. L. Strain Hardening and Strain Softening of Reversibly Cross-Linked Supramolecular Polymer Networks. *Macromolecules* **2011**, *44*, 7478–7488.
- (45) Herbert, K. M.; Getty, P. T.; Dolinski, N. D.; Hertzog, J. E.; de Jong, D.; Lettow, J. H.; Romulus, J.; Onorato, J. W.; Foster, E. M.; Rowan, S. J. Dynamic Reaction-Induced Phase Separation in Tunable, Adaptive Covalent Networks. *Chem. Sci.* **2020**, *11*, 5028–5036.
- (46) Sowan, N.; Cox, L. M.; Shah, P. K.; Song, H. B.; Stansbury, J. W.; Bowman, C. N. Dynamic Covalent Chemistry at Interfaces: Development of Tougher, Healable Composites through Stress Relaxation at the Resin–Silica Nanoparticles Interface. *Adv. Mater. Interfaces* **2018**, *5*, No. 1800511.

- (47) Chen, X.; Li, L.; Wei, T.; Venerus, D. C.; Torkelson, J. M. Reprocessable Polyhydroxyurethane Network Composites: Effect of Filler Surface Functionality on Cross-Link Density Recovery and Stress Relaxation. *ACS Appl. Mater. Interfaces* **2019**, *11*, 2398–2407.
- (48) Liu, Y.; Tang, Z.; Chen, Y.; Zhang, C.; Guo, B. Engineering of β -Hydroxyl Esters into Elastomer–Nanoparticle Interface toward Malleable, Robust, and Reprocessable Vitrimers Composites. *ACS Appl. Mater. Interfaces* **2018**, *10*, 2992–3001.
- (49) Legrand, A.; Soulié-Ziakovic, C. Silica–Epoxy Vitrimers Nanocomposites. *Macromolecules* **2016**, *49*, 5893–5902.
- (50) Cudjoe, E.; Herbert, K. M.; Rowan, S. J. Strong, Rebondable, Dynamic Cross-Linked Cellulose Nanocrystal Polymer Nanocomposite Adhesives. *ACS Appl. Mater. Interfaces* **2018**, *10*, 30723–30731.
- (51) Dominguez, M. N.; Howard, M. P.; Maier, J. M.; Valenzuela, S. A.; Sherman, Z. M.; Reuther, J. F.; Reimnitz, L. C.; Kang, J.; Cho, S. H.; Gibbs, S. L.; Menta, A. K.; Zhuang, D. L.; van der Stok, A.; Kline, S. J.; Anslyn, E. V.; Truskett, T. M.; Milliron, D. J. Assembly of Linked Nanocrystal Colloids by Reversible Covalent Bonds. *Chem. Mater.* **2020**, *32*, 10235–10245.
- (52) Borsley, S.; Kay, E. R. Dynamic Covalent Assembly and Disassembly of Nanoparticle Aggregates. *Chem. Commun.* **2016**, *52*, 9117–9120.
- (53) Wang, Y.; Santos, P. J.; Kubiak, J. M.; Guo, X.; Lee, M. S.; Macfarlane, R. J. Multistimuli Responsive Nanocomposite Tectons for Pathway Dependent Self-Assembly and Acceleration of Covalent Bond Formation. *J. Am. Chem. Soc.* **2019**, *141*, 13234–13243.
- (54) Nair, D. P.; Podgórski, M.; Chatani, S.; Gong, T.; Xi, W.; Fenoli, C. R.; Bowman, C. N. The Thiol–Michael Addition Click Reaction: A Powerful and Widely Used Tool in Materials Chemistry. *Chem. Mater.* **2014**, *26*, 724–744.
- (55) Serafimova, I. M.; Pufall, M. A.; Krishnan, S.; Duda, K.; Cohen, M. S.; Maglathlin, R. L.; McFarland, J. M.; Miller, R. M.; Frödin, M.; Taunton, J. Reversible Targeting of Nucleophilic Cysteines with Chemically Tuned Electrophiles. *Nat. Chem. Biol.* **2012**, *8*, 471–476.
- (56) Zhong, Y.; Xu, Y.; Anslyn, E. V. Studies of Reversible Conjugate Additions. *Eur. J. Org. Chem.* **2013**, *2013*, 5017–5021.
- (57) Krenke, E. H.; Petter, R. C.; Houk, K. N. Kinetics and Thermodynamics of Reversible Thiol Additions to Mono- and Diactivated Michael Acceptors: Implications for the Design of Drugs That Bind Covalently to Cysteines. *J. Org. Chem.* **2016**, *81*, 11726–11733.
- (58) Herbert, K. M.; Dolinski, N. D.; Boynton, N. R.; Murphy, J. G.; Lindberg, C. A.; Sibener, S. J.; Rowan, S. J. Controlling the Morphology of Dynamic Thia–Michael Networks to Target Pressure-Sensitive and Hot Melt Adhesives. *ACS Appl. Mater. Interfaces* **2021**, *13*, 27471–27480.
- (59) FitzSimons, T. M.; Oentoro, F.; Shanbhag, T. V.; Anslyn, E. V.; Rosales, A. M. Preferential Control of Forward Reaction Kinetics in Hydrogels Crosslinked with Reversible Conjugate Additions. *Macromolecules* **2020**, *53*, 3738–3746.
- (60) FitzSimons, T. M.; Anslyn, E. V.; Rosales, A. M. Effect of pH on the Properties of Hydrogels Cross-Linked Via Dynamic Thia–Michael Addition Bonds. *ACS Polym. Au* **2021**, *2*, 129–136.
- (61) Crucho, C. I. C.; Baleizão, C.; Farinha, J. P. S. Functional Group Coverage and Conversion Quantification in Nanostructured Silica by ^1H NMR. *Anal. Chem.* **2017**, *89*, 681–687.
- (62) Ewoldt, R. H.; Johnston, M. T.; Caretta, L. M. Experimental Challenges of Shear Rheology: How to Avoid Bad Data. In *Complex Fluids in Biological Systems: Experiment, Theory, and Computation* Spagnolie, S. E., Ed.; Springer: New York, NY, 2015; pp 207–241.
- (63) Coussot, P.; Nguyen, Q. D.; Huynh, H. T.; Bonn, D. Viscosity Bifurcation in Thixotropic, Yielding Fluids. *J. Rheol.* **2002**, *46*, 573–589.
- (64) Maas, J. H.; Fleer, G. J.; Leermakers, F. A. M.; Cohen Stuart, M. A. Wetting of a Polymer Brush by a Chemically Identical Polymer Melt: Phase Diagram and Film Stability. *Langmuir* **2002**, *18*, 8871–8880.
- (65) Green, D. L.; Mewis, J. Connecting the Wetting and Rheological Behaviors of Poly(Dimethylsiloxane)-Grafted Silica Spheres in Poly(Dimethylsiloxane) Melts. *Langmuir* **2006**, *22*, 9546–9553.
- (66) Dutta, N.; Green, D. Nanoparticle Stability in Semidilute and Concentrated Polymer Solutions. *Langmuir* **2008**, *24*, 5260–5269.
- (67) Banchio, A. J.; Heinen, M.; Holmqvist, P.; Nägele, G. Short- and Long-Time Diffusion and Dynamic Scaling in Suspensions of Charged Colloidal Particles. *J. Chem. Phys.* **2018**, *148*, No. 134902.
- (68) Dukes, D.; Li, Y.; Lewis, S.; Benicewicz, B.; Schädler, L.; Kumar, S. K. Conformational Transitions of Spherical Polymer Brushes: Synthesis, Characterization, and Theory. *Macromolecules* **2010**, *43*, 1564–1570.
- (69) Ohno, K.; Morinaga, T.; Takeno, S.; Tsujii, Y.; Fukuda, T. Suspensions of Silica Particles Grafted with Concentrated Polymer Brush: Effects of Graft Chain Length on Brush Layer Thickness and Colloidal Crystallization. *Macromolecules* **2007**, *40*, 9143–9150.
- (70) Pozzo, D. C.; Walker, L. M. Reversible Shear Gelation of Polymer–Clay Dispersions. *Colloids Surf., A* **2004**, *240*, 187–198.
- (71) Otsubo, Y.; Umea, K. Rheological Properties of Silica Suspensions in Polyacrylamide Solutions. *J. Rheol.* **1984**, *28*, 95–108.
- (72) Cabane, B.; Wong, K.; Lindner, P.; Lafuma, F. Shear Induced Gelation of Colloidal Dispersions. *J. Rheol.* **1997**, *41*, 531–547.
- (73) Zebrowski, J.; Prasad, V.; Zhang, W.; Walker, L. M.; Weitz, D. A. Shake-Gels: Shear-Induced Gelation of Laponite–PEO Mixtures. *Colloids Surf., A* **2003**, *213*, 189–197.
- (74) Collini, H.; Mohr, M.; Luckham, P.; Shan, J.; Russell, A. The Effects of Polymer Concentration, Shear Rate and Temperature on the Gelation Time of Aqueous Silica–Poly(Ethylene-Oxide) “Shake-Gels”. *J. Colloid Interface Sci.* **2018**, *517*, 1–8.
- (75) Kanai, H.; Amari, T. Negative Thixotropy in Ferric-Oxide Suspensions. *Rheol. Acta* **1995**, *34*, 303–310.
- (76) Yannas, J. B.; Gonzalez, R. N. A Clear Instance of Rheopectic Flow. *Nature* **1961**, *191*, 1384–1385.
- (77) Seto, R.; Mari, R.; Morris, J. F.; Denn, M. M. Discontinuous Shear Thickening of Frictional Hard-Sphere Suspensions. *Phys. Rev. Lett.* **2013**, *111*, No. 218301.
- (78) Hsu, C.-P.; Mandal, J.; Ramakrishna, S. N.; Spencer, N. D.; Isa, L. Exploring the Roles of Roughness, Friction and Adhesion in Discontinuous Shear Thickening by Means of Thermo-Responsive Particles. *Nat. Commun.* **2021**, *12*, No. 1477.
- (79) Maranzano, B. J.; Wagner, N. J. Flow-Small Angle Neutron Scattering Measurements of Colloidal Dispersion Microstructure Evolution through the Shear Thickening Transition. *J. Chem. Phys.* **2002**, *117*, 10291–10302.
- (80) Kersey, F. R.; Yount, W. C.; Craig, S. L. Single-Molecule Force Spectroscopy of Bimolecular Reactions: System Homology in the Mechanical Activation of Ligand Substitution Reactions. *J. Am. Chem. Soc.* **2006**, *128*, 3886–3887.
- (81) Kersey, F. R.; Loveless, D. M.; Craig, S. L. A Hybrid Polymer Gel with Controlled Rates of Cross-Link Rupture and Self-Repair. *J. R. Soc. Interface* **2007**, *4*, 373–380.